

Challenging

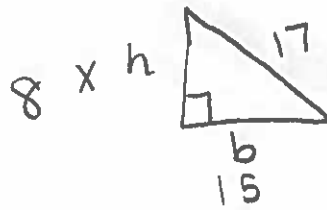
Name Answer Key

★ Pictures/Diagrams are NOT drawn to scale.

Work Area:

1. The area of a right triangle is 60 square inches and one leg is 15 inches. Determine the length of the hypotenuse.

hypotenuse = 17

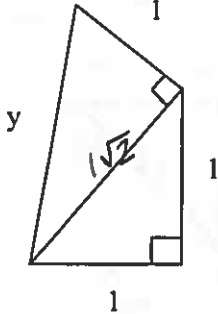


$$60 = \frac{15x}{2}$$

$$120 = 15x$$

$$8 = x$$

2. Find y



$$1^2 + (\sqrt{2})^2 = y^2$$

$$1 + 2 = y^2$$

$$3 = y^2$$

$\sqrt{3} = y$

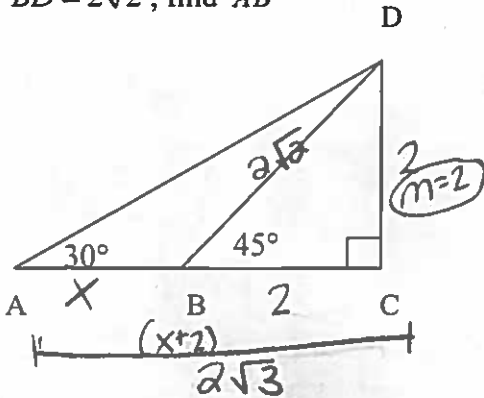
$$8^2 + 15^2 = c^2$$

$$64 + 225 = c^2$$

$$289 = c^2$$

$$17 = c$$

3. If $\overline{BD} = 2\sqrt{2}$, find \overline{AB}



45-45-90
m m m√2
x+2 = m

30-60-90
m m√3 2m

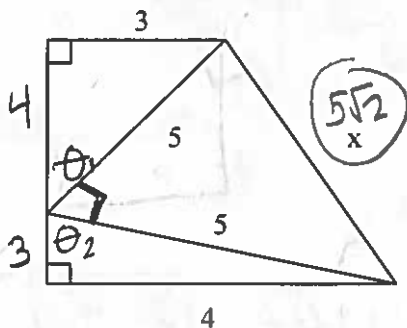
$$\tan 30 = \frac{2}{x+2}$$

$$x+2 = \frac{2}{\tan 30}$$

$$x = \frac{2}{\tan 30} - 2$$

$x = 2\sqrt{3} - 2 \approx 1.46$

4. Find x



$$\tan \theta_1 = \frac{3}{4}$$

$$\theta_1 \approx 36.87^\circ$$

$$\tan \theta_2 = \frac{4}{3}$$

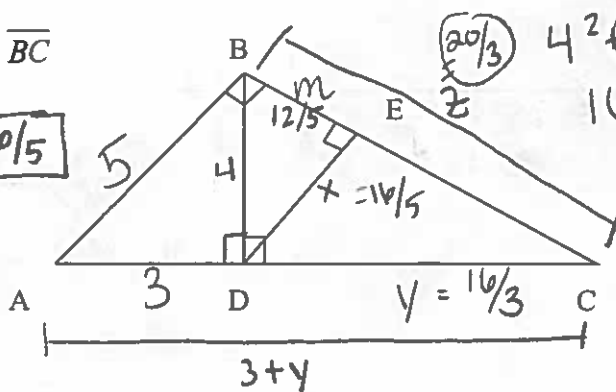
$$\theta_2 \approx 53.13^\circ$$

Complementary

$x = 5\sqrt{2}$

5. In $\triangle ABC$, $m\angle B = 90^\circ$
 $\overline{BD} \perp \overline{AC}$ and $\overline{DE} \perp \overline{BC}$
 $\overline{AB} = 5$ and $\overline{AD} = 3$
Find \overline{DE}

$DE = 10/5$



$$\frac{5}{3} = \frac{3+y}{5}$$

$$25 = 9 + 3y$$

$$16 = 3y \quad (y = 16/3)$$

$$4^2 + (16/3)^2 = z^2$$

$$16 + \frac{256}{9} = z^2$$

$$44 \frac{4}{9} = z^2$$

$$\sqrt{\frac{400}{9}} = z$$

$$\frac{20}{3} = z$$

$$\frac{4}{m} = \frac{20/3}{4}$$

$$16 = \frac{20}{3}m$$

$$\frac{12}{5} = m$$

$$x^2 + (\frac{12}{5})^2 = 4^2$$

$$x^2 + \frac{144}{25} = 16$$

$$x^2 = \frac{256}{25}$$

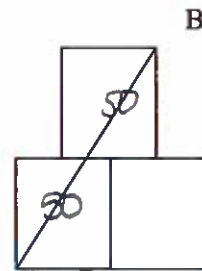
$$x = \frac{16}{5}$$

6. Three congruent squares are drawn as shown, in which the midpoints of two sides of the bottom squares are vertices of the top square. If $\overline{AB} = 100$, what is the area of one of these squares?

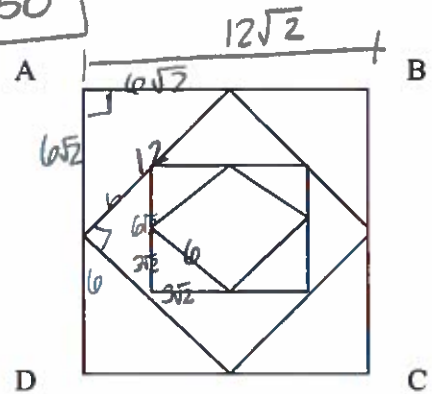
$$\frac{m\sqrt{2}}{\sqrt{2}} = \frac{50}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{50\sqrt{2}}{2} = 25\sqrt{2}$$

$$A = (25\sqrt{2})(25\sqrt{2})$$

$$A = 1250$$



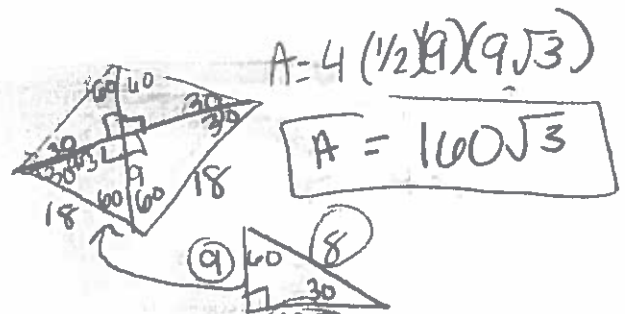
7. ABCD is a square with $AB = 12\sqrt{2}$ inches. Each of the inner figures is a square formed by connecting midpoints. What is the length of a side of the innermost square shown?



8. The perimeter of a rhombus containing a 120° angle is 72 cm. Determine the area of the rhombus.

$$P = 72$$

$$\text{Side length } 72/4 = 18$$



9. Given $m\angle CEB = 45^\circ$, $EC = 2$. Determine the sum of the perimeters of $\triangle ABE$ and $\triangle EDC$.

$$\frac{m\sqrt{2}}{\sqrt{2}} = \frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \sqrt{2}$$

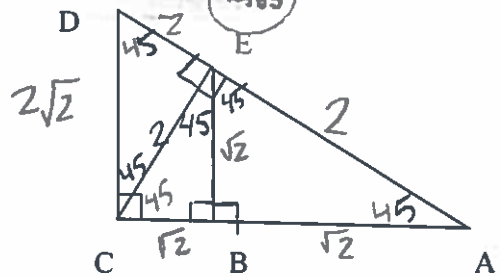
$$P_{\triangle ABE} = \sqrt{2} + \sqrt{2} + 2$$

$$2\sqrt{2} + 2$$

$$P_{\triangle EDC} = 2 + 2 + 2\sqrt{2}$$

$$4 + 2\sqrt{2}$$

$$\text{Sum} = 2\sqrt{2} + 2 + 4 + 2\sqrt{2} = 6 + 4\sqrt{2}$$



10. Given right $\triangle ABC$, with AD as an altitude, $AD = 5$, $m\angle DAB = 30^\circ$, determine AC , AB , BD , and DC .

$$\frac{m\sqrt{3}}{\sqrt{3}} = \frac{5}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{5\sqrt{3}}{3}$$

$$AC = 10$$

$$AB = \frac{10\sqrt{3}}{3}$$

$$BD = \frac{5\sqrt{3}}{3}$$

$$DC = 5\sqrt{3}$$

