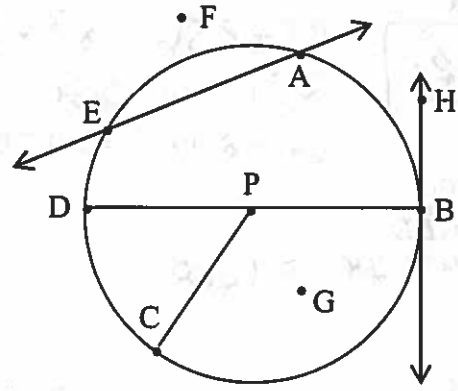


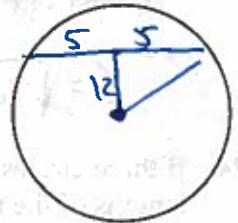
Use the diagram to the right to answer each of the following.

- Name the center of the circle. P
- Name the circle. ⊙P
- Name three radii of the circle. $\overline{PC}, \overline{PD}, \overline{PB}$
- Name the diameter of the circle. \overline{BD}
- Name a chord of the circle. $\overline{AE}, \overline{BD}$
- Name a tangent of the circle. \overleftrightarrow{BH}
- Name a secant of the circle. \overleftrightarrow{EA}
- Name two points in the interior of the circle. P & G
- Name two points in the exterior of the circle. F & H
- Name five points that lie on the circle. E, A, D, G, B
- Name a point of tangency. B
- Name a central angle. $\angle CPD$ & $\angle BPC$
- Name a semicircle: \widehat{BCD} , \widehat{BAD}
- Name two minor arcs. \widehat{AE} & \widehat{CD}
- Name two major arcs. \widehat{ABC} , \widehat{ADB} , ...



16. Given a chord of a circle is 10 inches long and is 12 inches from the center of the circle. Find the length of the radius.

triple! r = 13 in



17. Given an equilateral triangle is inscribed in ⊙Q with radius measuring 12 cm.

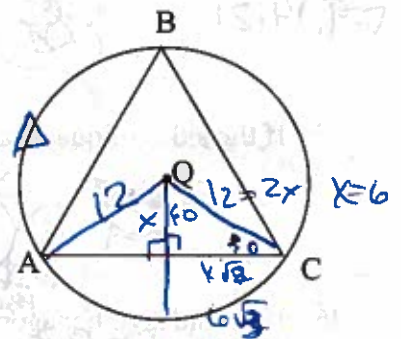
a. Find the length of each side of the equilateral triangle.

~~12√3~~
12√3 u

30-60-90 Δ

b. Find the distance from each side of the triangle to the center of the circle.

6 cm

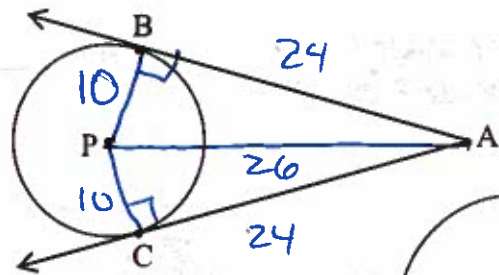


18. In the figure, both AC and AB are tangents to $\odot P$.

Given: $PB = 10$

$AP = 26$

Find: $AC = 24u$



19. Given: $\odot C$

Find: x

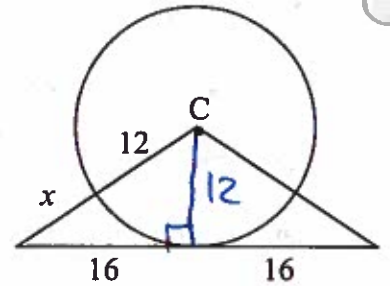
$x = 8$

$12^2 + 16^2 = (x+12)^2$

$144 + 256 = x^2 + 24x + 144$

$x^2 + 24x - 256 = 0$

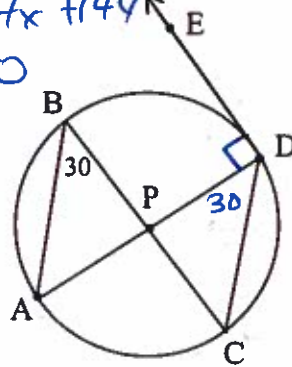
$(x-8)(x+32) = 0$



20. Given: $\odot P$

Tangent DE

Find: $m\angle EDC = 120^\circ$



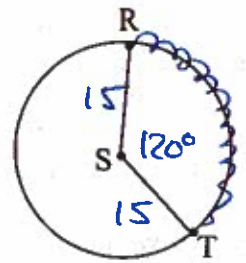
21. Given: $\odot S$

$m\angle RST = 120$

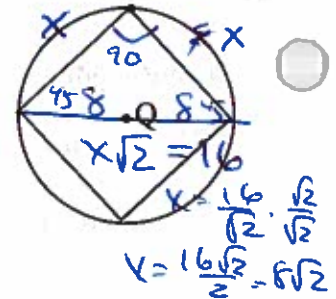
$ST = 15$

Find: a) length of \widehat{RT} b) area of sector RST

$l_{\widehat{RT}} = \frac{120}{360} 2\pi(15) = 10\pi u$ $A_{RST} = \frac{120}{360} \pi 15^2 = 75\pi u^2$



22. A square is inscribed in $\odot Q$. The diameter of the circle is 16 cm. Find the length of the side of the square. $8\sqrt{2} \text{ cm}$



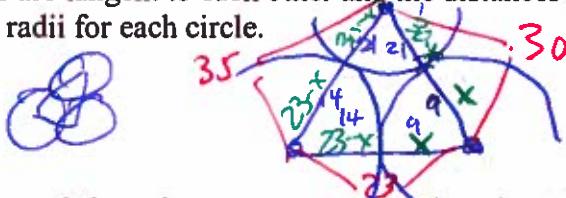
23. Find the area of a quadrilateral inscribed in a triangle with sides of 14, 16, 18, and 20.

Brahmagupta! $S = \frac{14+16+18+20}{2} = \frac{68}{2} = 34$

$A = \sqrt{20(18)(6)(4)} = \sqrt{80,640} = 48\sqrt{35} u^2$

24. If three circles are tangent to each other and the distances between the centers is 30, 23, and 37, find the lengths of the radii for each circle.

$r = 9, 14, 21$



$23 - x + 30 - x = 35$

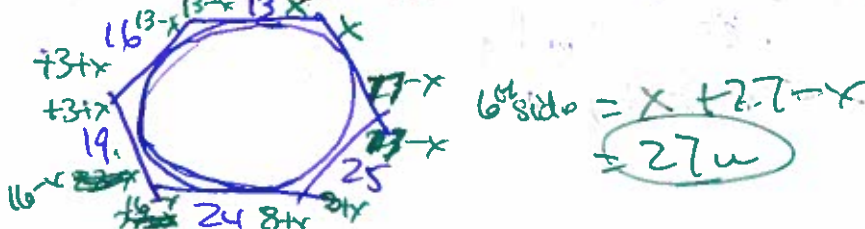
$53 - 2x = 35$

$-2x = -18 \quad x = 9$

25. If the sides of quadrilateral that has an inscribed circle and sides of 13, 16, and 25, find the remaining side.

$x + 22 - x = 22u$

26. If the sides of hexagon that has an inscribed circle and sides of 13, 16, 19, 24, and 25, find the 6th side.



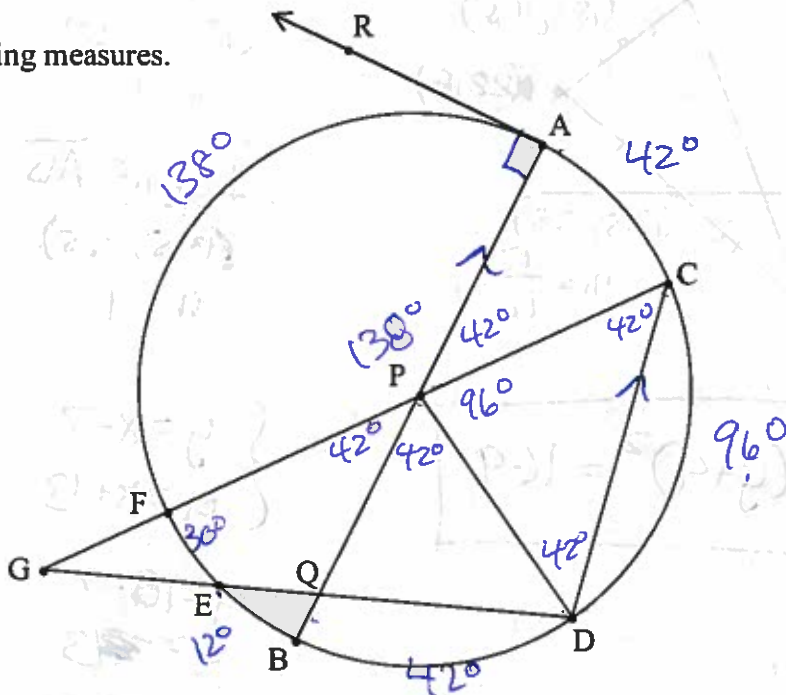
6th side = $x + 27 - x = 27u$

27. In $\odot P$, $AB \parallel CD$, AR is tangent to $\odot P$ at A .

$$m\widehat{BD} = 42^\circ$$

$$m\widehat{BE} = 12^\circ$$

Find each of the following measures.



- | | | | | | |
|----|-----------------|-------------|----|-----------------|-------------|
| a. | $m\angle BPD$ | <u>42°</u> | g. | $m\widehat{CD}$ | <u>96°</u> |
| b. | $m\angle APC$ | <u>42°</u> | h. | $m\widehat{FB}$ | <u>42°</u> |
| c. | $m\angle BPF$ | <u>42°</u> | i. | $m\widehat{FE}$ | <u>30°</u> |
| d. | $m\widehat{AF}$ | <u>138°</u> | j. | $m\angle EDC$ | <u>105°</u> |
| e. | $m\angle FCD$ | <u>42°</u> | k. | $m\angle G$ | <u>33°</u> |
| f. | $m\widehat{AC}$ | <u>42°</u> | l. | $m\angle EQB$ | <u>75°</u> |
| | | | m. | $m\angle RAB$ | <u>90°</u> |

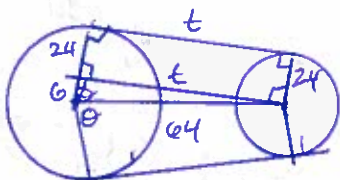
28. Find the belt length need for 2 pulleys with radii of 24 and 30 cm that are 10 cm apart.

$$L_{\text{belt}} = 2t + \text{Arc}_{\text{Big}} + \text{Arc}_{\text{Small}}$$

$$= 2(63.71813) + 99.58105 + 70.89161$$

$$= 298.2089$$

$\approx 298 \text{ cm}$



$$t^2 + 6^2 = 64^2$$

$$t^2 + 36 = 4096$$

$$\sqrt{t^2} = \sqrt{4060}$$

$$t = 63.71813$$

$$\cos \theta = \frac{6}{64}$$

$$\theta = 84.6286$$

$$2\theta = 169.24124$$

$$\text{Arc}_{\text{Big}} = \frac{2\pi r}{360}$$

$$= \frac{2\pi(30)}{360}$$

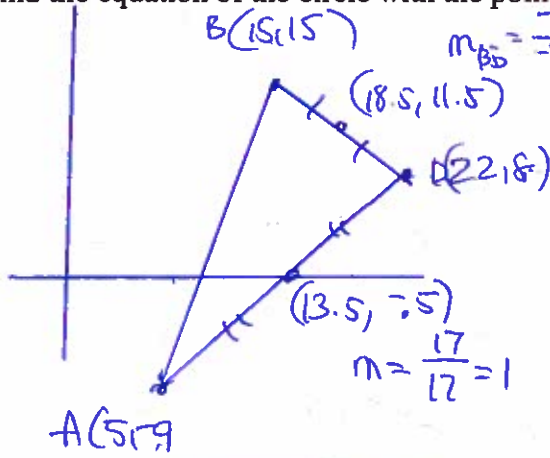
$$= \frac{190.7588}{360} 2\pi(30)$$

$$= 99.58105$$

$$\text{Arc}_{\text{Small}} = \frac{169.24124}{360} 2\pi(24)$$

$$= 70.89161$$

29. Find the equation of the circle with the points (15, 15), (22, 8), and (5, -9).



⊥ bis of \overline{BD}
(18.5, 11.5)
 $m = 1$

$$y - 11.5 = 1(x - 18.5)$$

$$y = x - 7$$

⊥ bis of \overline{AD}
(13.5, -5)
 $m = -1$

$$y + 5 = -1(x - 13.5)$$

$$y = -x + 13$$

$$\begin{cases} y = x - 7 \\ y = x + 13 \end{cases}$$

$$x - 7 = x + 13$$

$$2x = 20$$

$$x = 10 \text{ center}$$

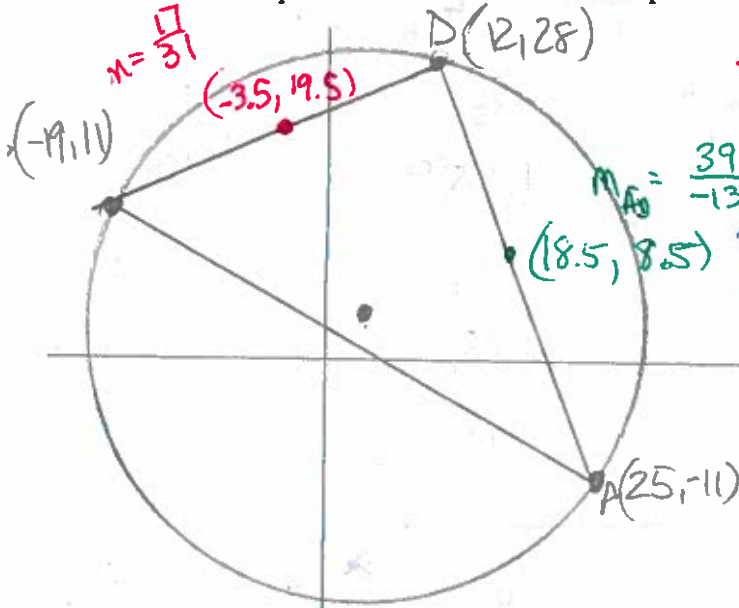
$$y = 10 - 7$$

$$y = 3$$

$$(10, 3)$$

using (15, 15), $r = \sqrt{\frac{15^2 + 15^2}{25 + 144}} = \sqrt{169} = 13$ radius

30. Find the equation of the circle with the points (25, -11), (-19, 11), and (12, 28).



⊥ bis. of \overline{BD}
(-3.5, 19.5)
 $m = -\frac{31}{17}$

$$y - 19.5 = -\frac{31}{17}(x - 19.5)$$

$$y - \frac{39}{2} = -\frac{31}{17}x + \frac{-217}{34}$$

$$+ \frac{39}{2} \quad \frac{663 + 32}{34}$$

$$(x - 5)^2 + (y - 4)^2 = 625$$

$$y = -\frac{31}{17}x + \frac{446}{34}$$

$$y = -\frac{31}{17}x + \frac{223}{17}$$

⊥ bis of \overline{AD}
(18.5, 8.5)
 $m = -\frac{39}{13} = -3$
 $m = 1/3$

$$y - 8.5 = \frac{1}{3}(x - 18.5)$$

$$y - 8.5 = \frac{1}{3}x - \frac{37}{6}$$

$$y - \frac{17}{2} = \frac{1}{3}x - \frac{37}{6}$$

$$+ \frac{17}{2} \quad + \frac{17}{6} + \frac{17}{2}$$

$$y = \frac{1}{3}x + \frac{14}{6}$$

$$y = \frac{1}{3}x + \frac{7}{3}$$

$$\begin{cases} y = -\frac{31}{17}x + \frac{223}{17} \\ y = \frac{1}{3}x + \frac{7}{3} \end{cases}$$

$$17y = -31(3y - 7) + 223$$

$$17y = -93y + 217 + 223$$

$$110y = 440$$

$$y = 4!$$

$$y = \frac{1}{3}(\quad) + \frac{7}{3}$$

$$y = \frac{4}{3} + \frac{7}{3}$$

$$x = 3(4) - 7 = 5!$$

$$C(5, 4)$$

$$r = \sqrt{49 + 576} = \sqrt{625} = 25 = r$$

$$\begin{cases} 17y = -31x + 223 \\ 3y = x + 7 \\ x = 3y - 7 \end{cases}$$